

## **Mathematical Methods of Automation and Robotics**

### **exam issues**

- 1.** Inverse function theorem
- 2.** Implicit function theorem
- 3.** Equivalence of functions
- 4.** Theorem on immersions and submersions
- 5.** Local and global diffeomorphism
- 6.** Morse theorem
- 7.** Contraction functions theorem
- 8.** Dynamic system, flow: theorem on existence and uniqueness of solution
- 9.** Stability: Ważewski inequality
- 10.** Stability: Lyapunov function
- 11.** Equivalence of dynamic systems
- 12.** Linearization of dynamic systems: theorem of Hartmann-Grobman
- 13.** Linearization of dynamic systems: theorem of Poincare'-Siegel-Sternberg
- 14.** Lie brackets of vector fields, definition and properties
- 15.** Theorems of straightening out a vector field and a family of vector fields
- 16.** Distributions and Frobenius theorem
- 17.** Controllability of nonlinear systems: definitions and criteria
- 18.** Equivalence of control affine systems
- 19.** Feedback linearization: theorem of Jakubczyk-Respondek
- 20.** Input-output decoupling, system structure, zero dynamics
- 21.** Dynamic feedback linearization: theorem of Charlet-Levine-Marino
- 22.** Differentially flat systems

**Please, have a copy of these issues on the exam.**

#### **BASIC REFERENCES**

- [1] M. Golubitsky, V. Guillemin „Stable Mappings and Their Singularities”, Springer-Verlag, New York, 1974
- [2] R. Abraham, J. E. Marsden, T. Ratiu „Manifolds, Tensor Analysis, and Applications”, Springer-Verlag, New York, 1988
- [3] V. I. Arnold „Geometrical Methods in the Theory of Ordinary Differential Equations”, Springer-Verlag, New York, 1983
- [4] S. S. Sastry „Nonlinear Systems”, Springer-Verlag, New York, 1999
- [5] A. M. Bloch „Nonholonomic Mechanics and Control”, Springer-Verlag, New York, 2003
- [6] H. Nijmeijer, A. J. van der Schaft „Nonlinear Dynamical Control Systems”, Springer-Verlag, New York, 1990
- [7] J. Levine „Analysis and Control of Nonlinear Systems”, Springer, New York, 2009
- [8] K. Tchoń, R. Muszyński „MMAR, Lecture Notes”, Wrocław, 2019.

#### **COMPLEMENTARY REFERENCES**

- [1] Ph. Hartman „Ordinary Differential Equations”, J. Wiley, New York, 1964
- [2] H. K. Khalil „Nonlinear Systems”, Prentice-Hall, New Jersey, 2000
- [3] R. Murray, Z. Li, S. S. Sastry „A Mathematical Introduction to Robotic Manipulation”, CRC Press, Boca Raton, 1994
- [4] A. Isidori „Nonlinear Control Systems”, Springer-Verlag, New York, 1995
- [5] V. Jurdjevic „Geometric Control Theory”, Cambridge Univ. Press, Cambridge, 1997